

Point-spread function model for fluorescence MACROscopy imaging

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PSF model for
MACROscopy

P.
Pankajakshan,
et al.

Road map

MACROscope

Point-spread
function

Scalar model

Numerical
results

- 1 MACROscope
- 2 Point-spread function
- 3 Scalar PSF model
- 4 Numerical results

MACROscope-Best of the two worlds

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Figure 1: Leica MACROFLuo™

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What is claimed?

- ▶ large object fields (up to 35mm),



Figure 1: Leica MACROFLuo™

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- ▶ large object fields (up to 35mm),
- ▶ large working distances (up to 97mm),



Figure 1: Leica MACROFLuo™

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- ▶ large object fields (up to 35mm),
- ▶ large working distances (up to 97mm),
- ▶ **parallax-free** and precise imaging,



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- ▶ large object fields (up to 35mm),
- ▶ large working distances (up to 97mm),
- ▶ **parallax-free** and precise imaging,
- ▶ multi-color fluorescence at high resolution.



Figure 1: Leica MACROFLuo™

The "Why?"

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- ▶ Biological specimens
often **scatter light**,

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- ▶ Biological specimens often **scatter light**,
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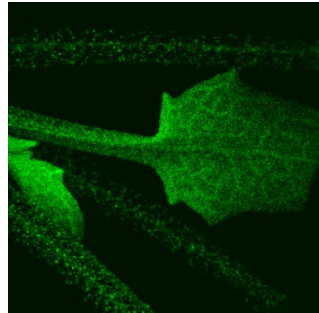


Figure 2: Confocal MACROscope image of *Arabidopsis Thaliana* seedlings ©INRA Sophia Antipolis, France.

Numerical aperture and resolution

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Numerical aperture and resolution

$$\text{NA} = n_i \sin \theta_{\max}$$

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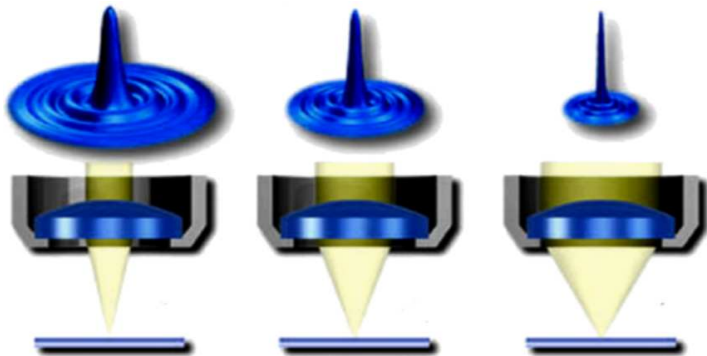


Figure 3: Numerical aperture and resolution for microscope.

Numerical aperture and working distance

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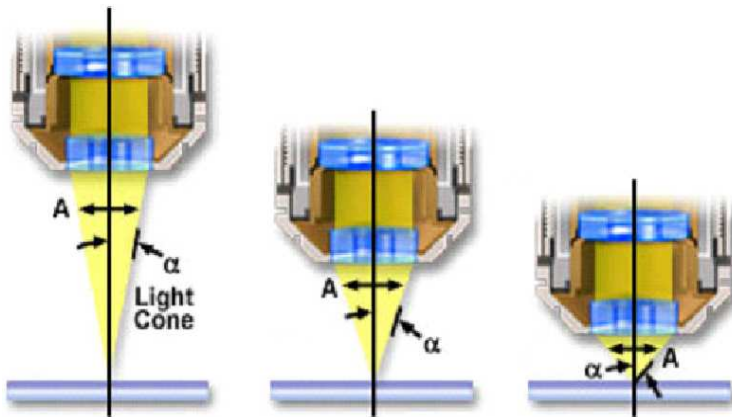


Figure 4: Schema of numerical aperture influencing working distance.

Why do we need a point-spread function (PSF)?

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Figure 5: Confocal MACROscope image of *Arabidopsis Thaliana* seedlings
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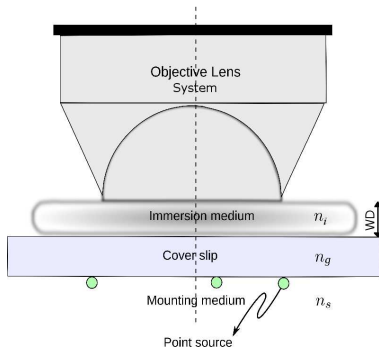


Figure 6: Experimental determination of the impulse response of the MACROscope by imaging point sources.

Experiments on the MACROscope

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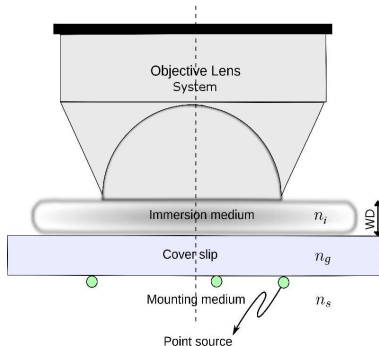


Figure 6: Experimental determination of the impulse response of the MACROscope by imaging point sources.

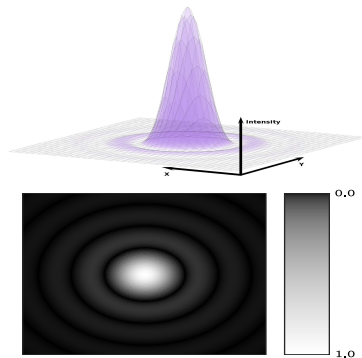


Figure 7: 2D Airy disk function.

MACROscopes-Are they really the best of the two worlds?



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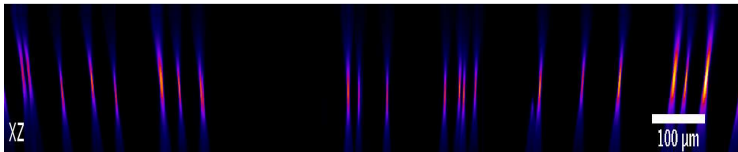


Figure 8: Radial projection of $4\mu\text{m}$ beads as imaged from a Leica Widefield MacroFluoTM Z16 APO. The objective has a 5X magnification and a zoom of up to 16X. ©Herbomel lab, Pasteur Institute.

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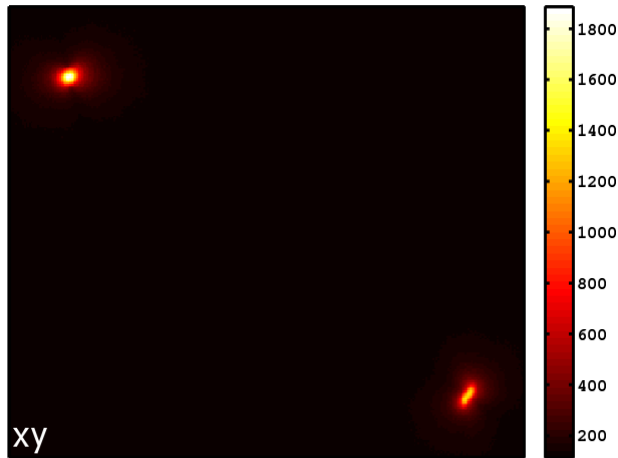


Figure 9: Axial projection of 4μm beads as imaged from a Leica Widefield MacroFluo™ Z16 APO. The objective has a 5X magnification and a zoom of 1.6X. ©Herbomel lab, Pasteur Institute.

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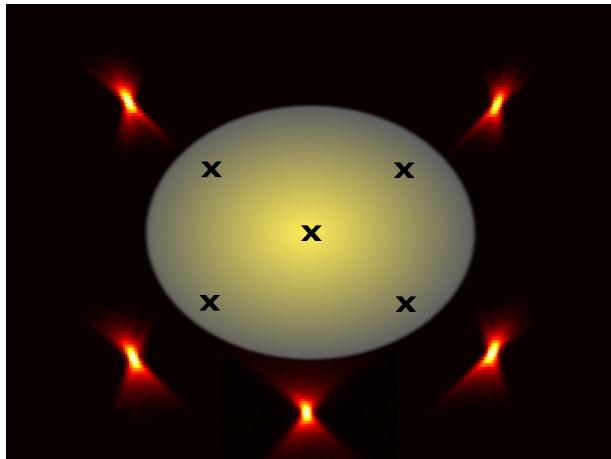


Figure 10: Bead images taken at different lateral positions of the field (as marked by the cross).

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- ▶ When the acquisition parameters are known, **restoration** can be achieved by using either theoretically calculated or estimated PSFs.

Incoherent scalar PSF model

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- ▶ When the acquisition parameters are known, **restoration** can be achieved by using either theoretically calculated or estimated PSFs.
- ▶ If $P(k_x, k_y, z)$ is the 2D **complex pupil function** and λ is the wavelength, the amplitude PSF can be calculated by just $2N_z$ number of 2D FFTs

$$h_A(x, y, z; \lambda) = \int_{k_x} \int_{k_y} P(k_x, k_y, z) \exp(j(k_x x + k_y y)) dk_y dk_x$$

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- ▶ and the **incoherent PSF** is

$$h_{Th}(\mathbf{x}; \lambda_{ex}, \lambda_{em}) = C |h_A(\mathbf{x}; \lambda_{ex})| \times |h_A(\mathbf{x}; \lambda_{em})|$$

Asilomar coffee cup

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Figure 11: Out-of-focus highlights (OOFH) for the Asilomar coffee cup.
(Photograph by Praveen Pankajakshan.)

Cat's eye effect

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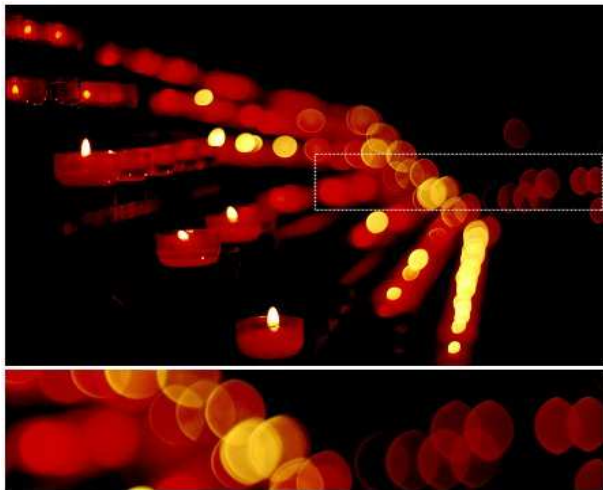


Figure 12: The Cat's eye effect is seen in the out-of-focus highlights (OOFH).
(Photograph by Peter Boehmer.)

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Figure 13: Lens viewed from the front.
(Photograph by Peter Boehmer.)

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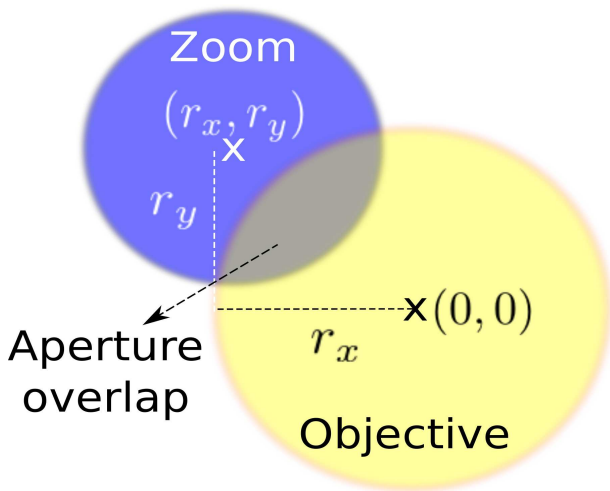


Figure 13: Lens viewed from the front.
(Photograph by Peter Boehmer.)



Figure 14: Lens viewed from the side.
(Photograph by Peter Boehmer.)

Limiting apertures overlapping



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Pacific grove beach at no zoom

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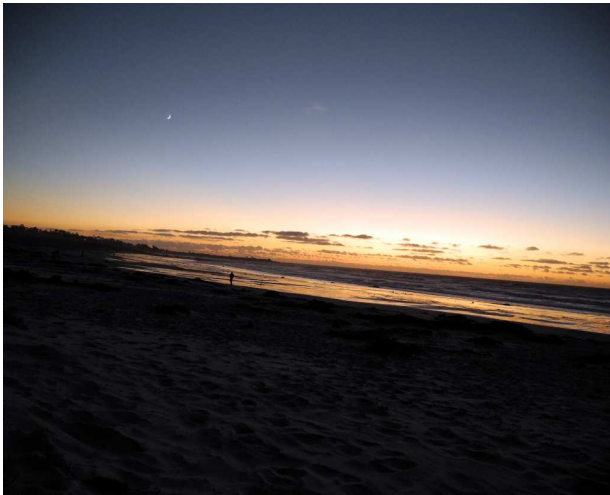


Figure 15: Optical vignetting example at minimum zoom. (Photograph by Praveen Pankajakshan.)

Pacific grove beach zoom position 1×

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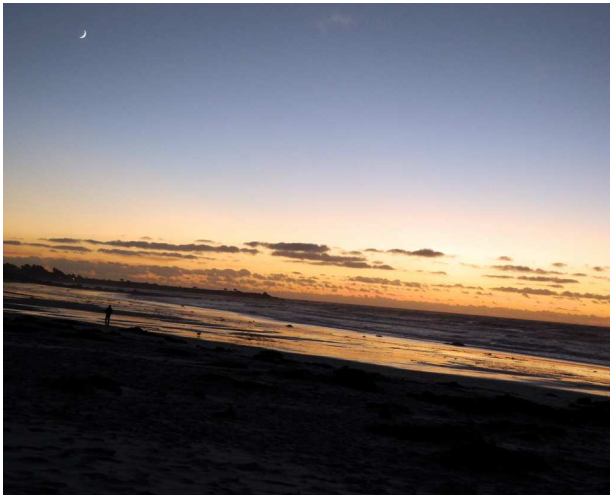


Figure 16: Optical vignetting disappears as zoom is increased. (Photograph by Praveen Pankajakshan.)

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- ▶ For a MICROscope, the **pupil function** is

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- For a MICROscope, the **pupil function** is

$$P_m(k_x, k_y, z; \lambda) = \begin{cases} e^{jk_0\phi(\theta_i, \theta_s, z)}, & \text{if } \sqrt{k_x^2 + k_y^2} < \frac{2\pi}{\lambda} \text{NA}_{\text{Obj}} \\ 0, & \text{otherwise.} \end{cases}$$

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- ▶ modification for a MACROscope

$$P(k_x, k_y, z; \lambda) = \begin{cases} \textcolor{red}{P}_m, & \text{if } \sqrt{(k_x - r_x)^2 + (k_y - r_y)^2} < \frac{2\pi}{\lambda} \text{NA}_{\text{Zo}} \\ \textcolor{red}{0}, & \text{otherwise.} \end{cases}$$

- ▶ For a MICROscope, the **pupil function** is

$$P_m(k_x, k_y, z; \lambda) = \begin{cases} e^{jk_0\phi(\theta_i, \theta_s, z)}, & \text{if } \sqrt{k_x^2 + k_y^2} < \frac{2\pi}{\lambda} \text{NA}_{\text{Obj}} \\ 0, & \text{otherwise.} \end{cases}$$

- ▶ modification for a MACROscope

$$P(k_x, k_y, z; \lambda) = \begin{cases} P_m, & \text{if } \sqrt{(k_x - r_x)^2 + (k_y - r_y)^2} < \frac{2\pi}{\lambda} \text{NA}_{\text{Zo}} \\ 0, & \text{otherwise.} \end{cases}$$

- ▶ **parameters** of the PSF: $\omega_h = \{\text{NA}_{\text{Obj}}, \text{NA}_{\text{Zo}}, r_x, r_y\}$

Compare experimental PSF and theoretical PSF

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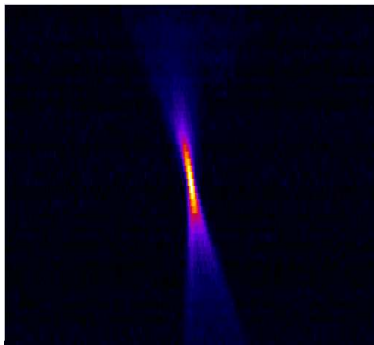


Figure 17: Experimental image of point source. Bead diameter $4\mu\text{m}$ and zoom 1X. ©Imaging Center, IGBMC, France.

Compare experimental PSF and theoretical PSF

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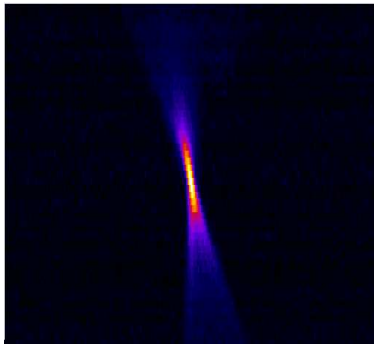


Figure 17: Experimental image of point source. Bead diameter $4\mu\text{m}$ and zoom 1X. ©Imaging Center, IGBMC, France.

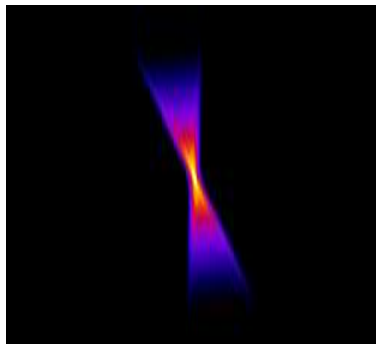


Figure 18: Simulated image of point source assuming the maximum NA of 0.5.

Optically vignetting the pupil

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Figure 19: Simulating the vignetting.

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Figure 19: Simulating the vignetting.

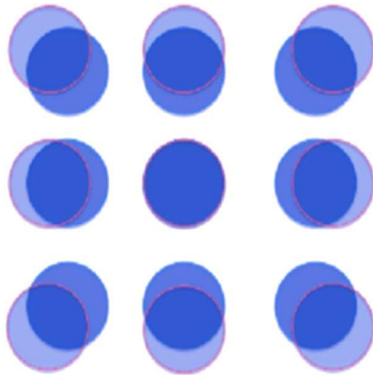


Figure 20: Schematic of overlapping apertures.

Degree of vignetting

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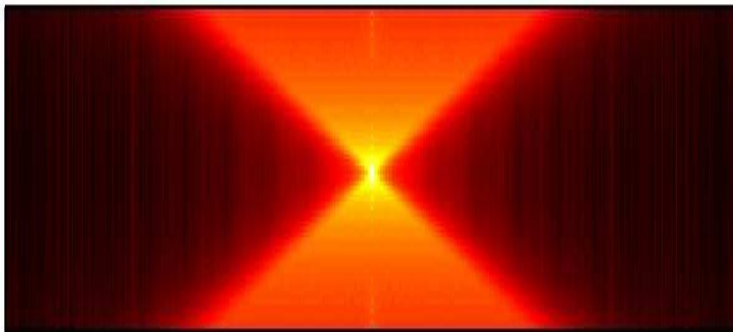


Figure 21: Simulated image of point source assuming **100% overlap** of the apertures.

Degree of vignetting

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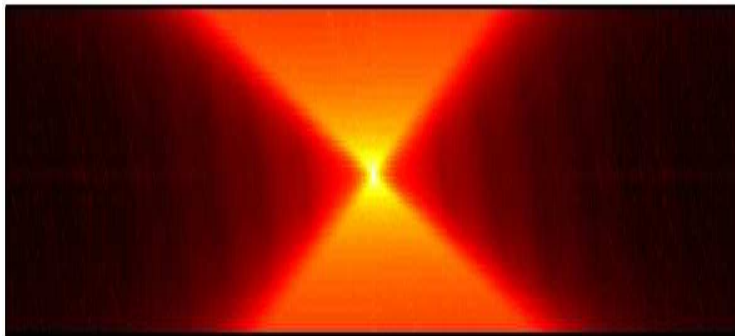


Figure 22: Simulated image of point source assuming an **overlap of 75%** of the apertures.

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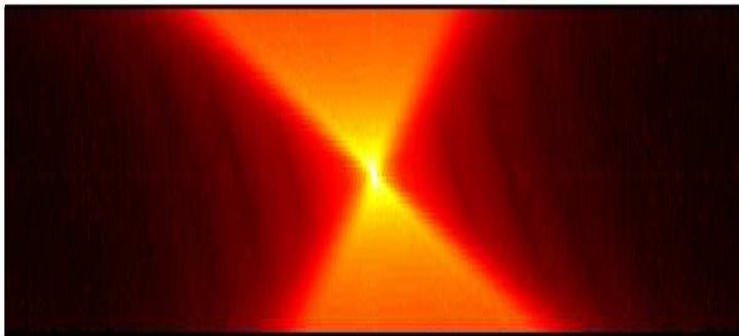


Figure 23: Simulated image of point source assuming an **overlap of 50%** of the apertures.

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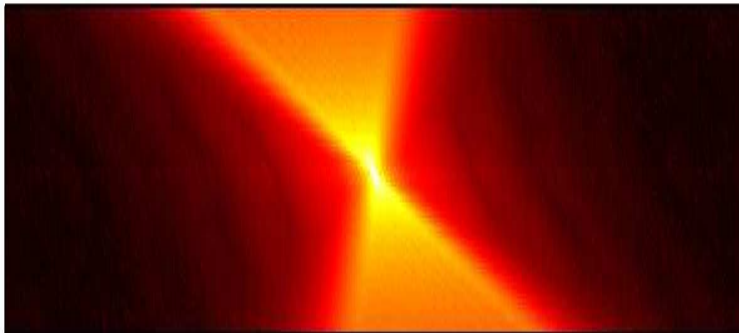


Figure 24: Simulated image of point source assuming an **overlap of 25%** of the apertures.

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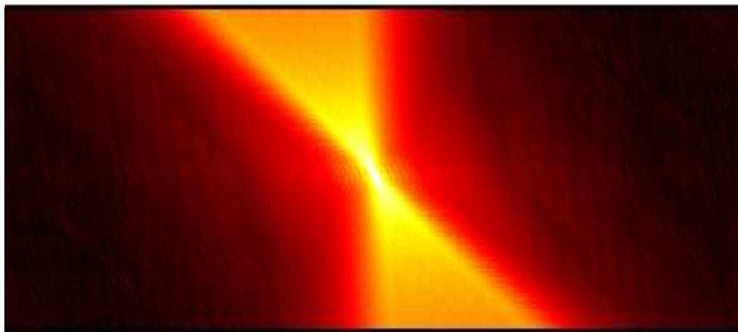


Figure 25: Simulated image of point source assuming an **overlap of 10%** of the apertures.

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- ▶ MACROscope PSF varies as a function of the **lateral position**,

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- ▶ the **initial PSF model** will be enhanced further with newer acquisitions on different systems,

- ▶ MACROscope PSF varies as a function of the **lateral position**,
- ▶ **vignetting** was observable only for smaller zooms (large FOV),
- ▶ the **initial PSF model** will be enhanced further with newer acquisitions on different systems,
- ▶ **restoration of images** can be achieved with the complete or partial knowledge of the theoretical PSF.

- ▶ The first author wish to thank ANR DIAMOND for funding the postdoctoral research fellowship,
- ▶ the authors are grateful to Dr. Philippe Herbomel from the Institut Pasteur, France and Dr. Didier Hentsch from IGBMC, France for the images and the discussions,
- ▶ some of the slides in this presentation were prepared by Dr. Mickael Lelek from Institut Pasteur, France, a big thanks to him,
- ▶ we acknowledge our colleagues for their support.

For more information see:

<http://www-syscom.univ-mlv.fr/ANRDIAMOND/>.