

Deconvolved phase imaging for diffraction tomography

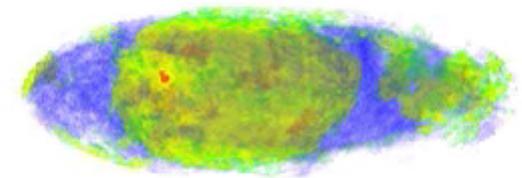
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New tomographic method:
Optical diffraction tomography for microscopy...
... a good tool for 3D imaging of biological cells.

- Transparent objects imaging in 3D thanks to phase information.
- Non invasive and label free.
- Based on digital holographic microscopy (DHM).
- Physical interaction between light and matter is considered.



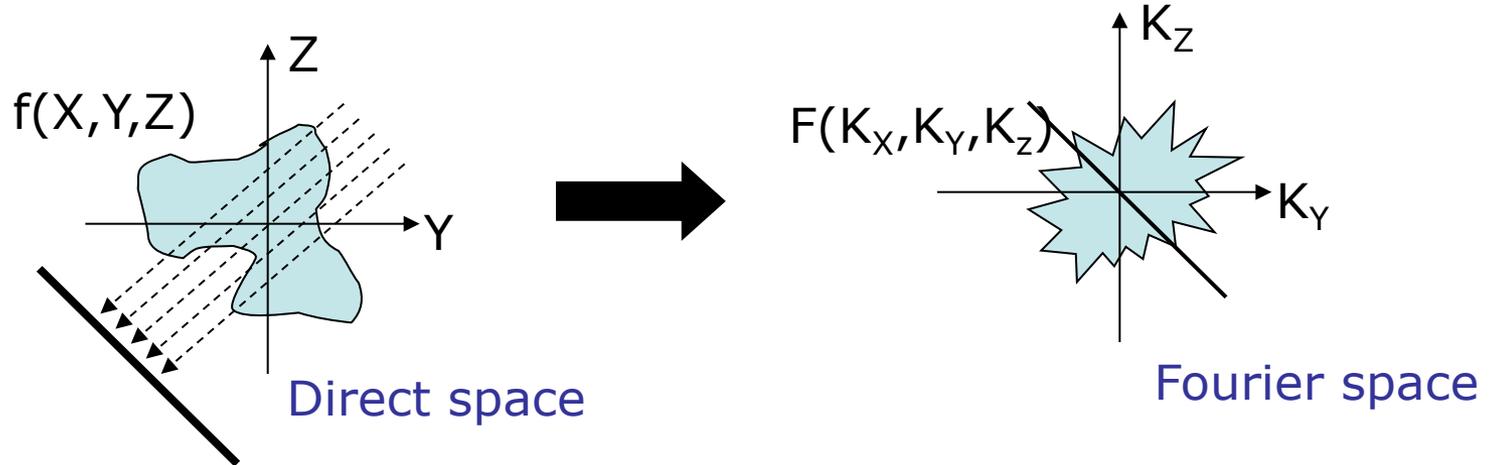
To help achieving high resolution:
3D complex deconvolution method is applied!

F. Charrière, et al., Living specimen tomography by digital holographic microscopy: morphometry of testate amoeba. *Optics Express*, 14(16):7005-7013, 2006.

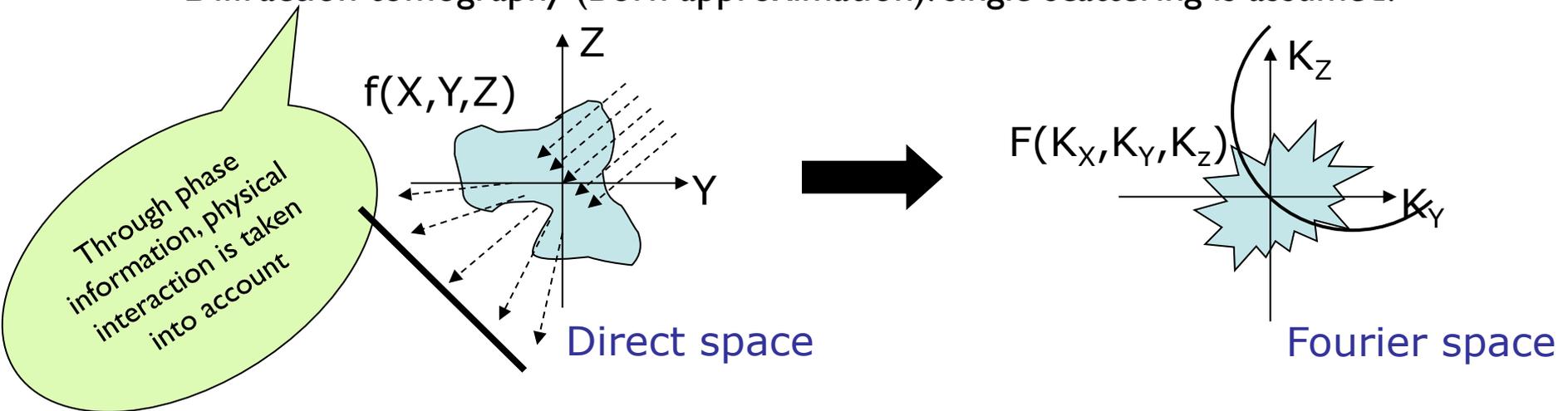
II. PRINCIPLES

Diffraction tomography

- Backprojection (Radon): light is considered travelling along straight rays.



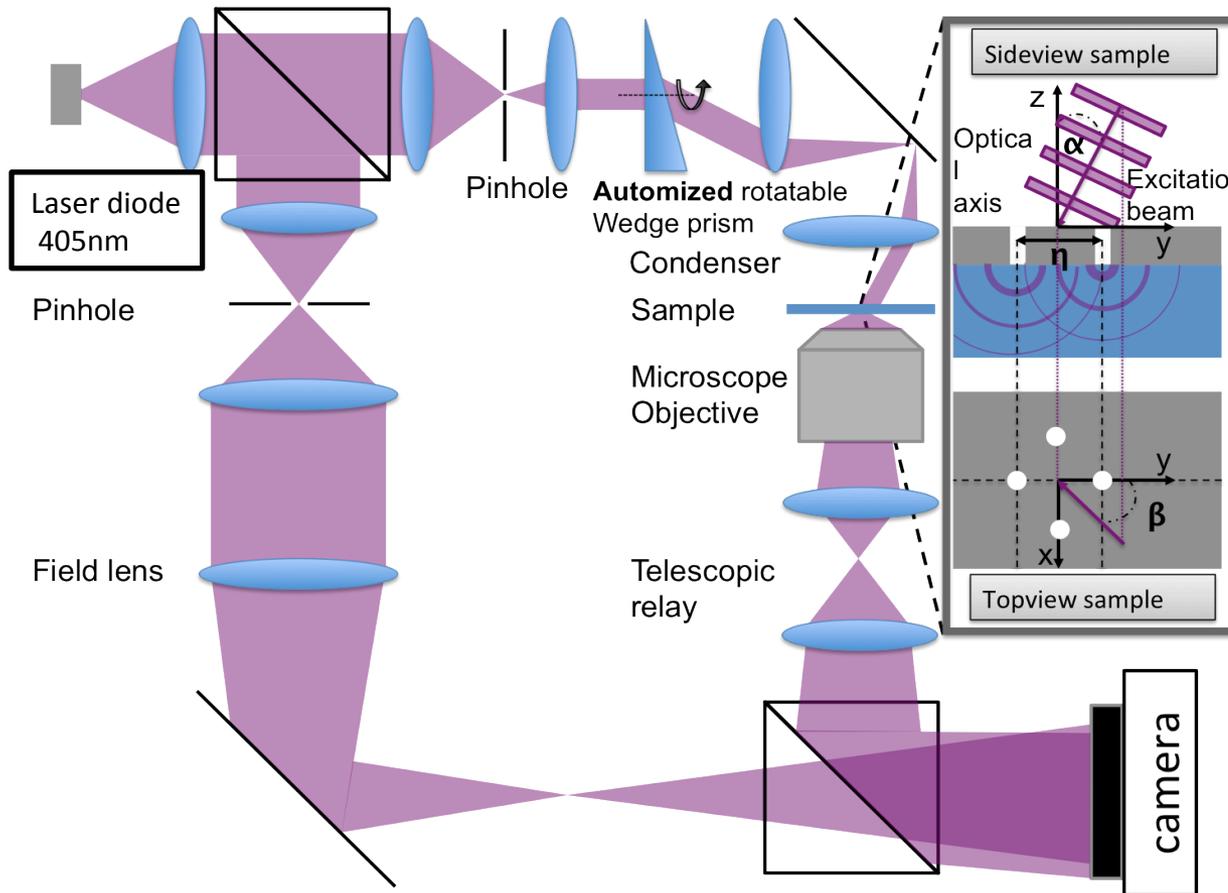
- Diffraction tomography (Born approximation): single scattering is assumed.



Devaney, "A filtered backpropagation algorithm for diffraction tomography," Ultrasonic Imaging 4(4), 336–350 (1982).

II. PRINCIPLES

Angular beam scanning holographic microscopy



Wavelength
405nm

Microscope objectives
 $NA_{MO}=1.4$ (oil)

Condenser
 $NA_{Cond}=0.4$ (air)

Wedge prism
scanning 1°

Relay magnification
Sampling=22nm

Cotte Y. et al., Journal of Biomedical Optics 16(10), 106007 (2011)

Fig. ▲ In DHM transmission configuration, a rotatable wedge prism is used to tune illumination conditions. The inset illustrates excitation beam's orientation in side and top perspective of the test target. The beam propagates in the direction of β (arrow: k -vector) and is inclined by angle α .

II. PRINCIPLES

High-resolution imaging

To achieve higher spatial 3D resolution:

- higher **NA**
- shorter **wavelength**
- **steeper tomographic angles** (sample/illumination rotation)

Problem:

Measured field Incident field scattered field

Extraction of scattered field
From diffraction theory

$$U(\vec{r}_1) = U^{(i)}(\vec{r}_1) + U^{(s)}(\vec{r}_1)$$

Object field

Coherent image formation

$$U(\vec{r}_2) = \iiint_{-\infty}^{\infty} o(\vec{r}_1) h(\vec{r}_2 - \vec{r}_1) dx_1 dy_1 dz_1,$$

Object
reconstruction
in reciprocal space:

$$FT_{3D}[F] = \frac{f_z}{2\pi} \left(FT_{2D}[o^{(s)}] \right) e^{-i2\pi f_z z}$$

Object scattering potential

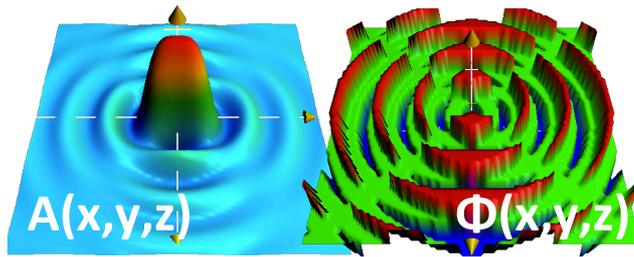
Scattered object field

Field convolved with
APSF
=> We need scattered
object field
=> Important for high-
resolution!

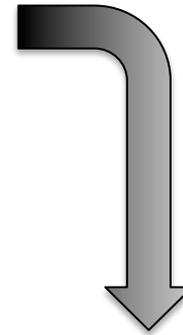
III. 3D COMPLEX DECONVOLUTION

Coherent image inversion

complex image
 $U(x_2, y_2)$



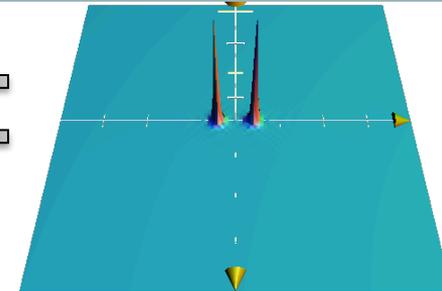
FFT



complex spectrum

Inverse filtering

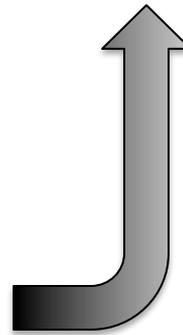
- + physical method:
Inversion of imaging formation
- noise amplification
- phase loss



*deconvolution theorem
for coherent imaging*

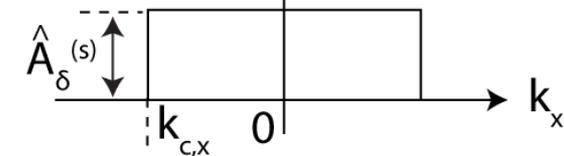
$$o(\vec{r}_1) = \iiint_{-\infty}^{\infty} O(\vec{k}) \exp[-i2\pi(\vec{k} \cdot \vec{r}_1)] dk_x dk_y dk_z = \mathcal{F}^{-1} \left\{ \frac{G(\vec{k})}{c(\vec{k})} \right\}$$

Coherent transfer function
(CTF)

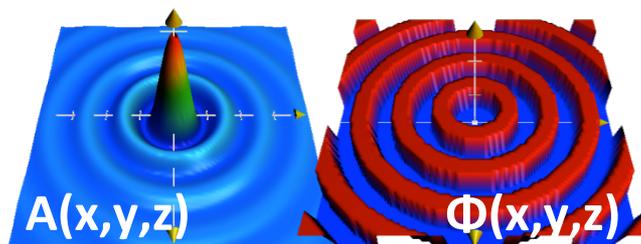


FFT

transmission



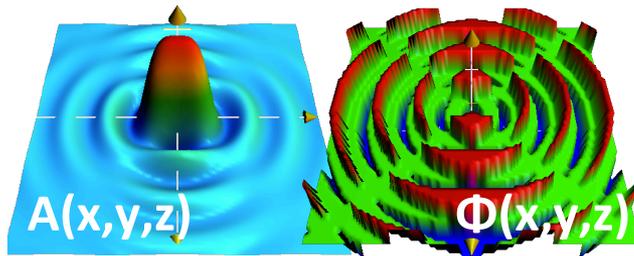
complex point
spread function
(APSF)
 $h(x_2, y_2)$



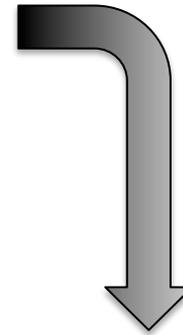
III. 3D COMPLEX DECONVOLUTION

3D filtering

complex image
 $U(x_2, y_2)$

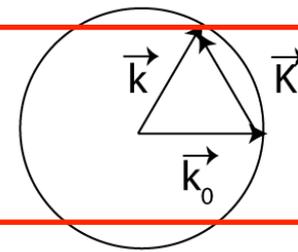


FFT

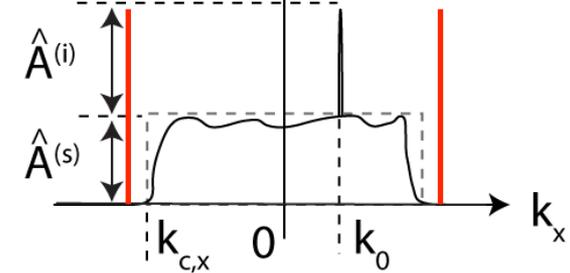


complex spectrum

Problem: In 3D



transmission



w\ low pass filter

Complex regularization

- + noise suppression 3D
- + no phase loss

w\ complex regularization

*deconvolution theorem
for coherent imaging*

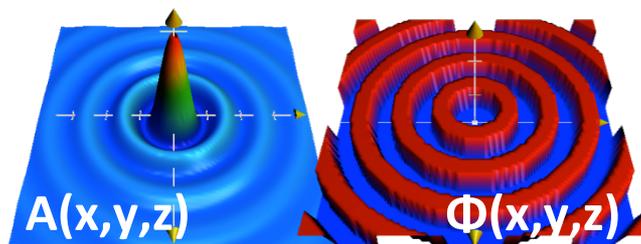
$$o(\vec{r}_1) = \mathcal{F}^{-1} \left\{ \frac{G(\vec{k})}{c(\vec{k})} \right\}$$

$$\tilde{c}(\vec{k}) = \begin{cases} c & \text{if } |c| > \tau \\ 1 \cdot \exp[i \cdot \arg[c]] & \text{if } |c| \leq \tau \end{cases}$$

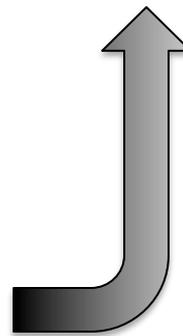
Coherent transfer function
(CTF)

w\ complex regularization

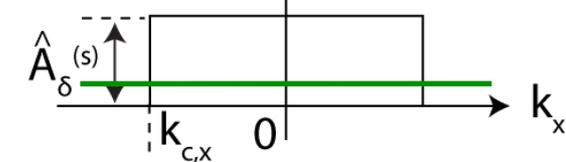
complex point
spread function
(APSF)
 $h(x_2, y_2)$



FFT

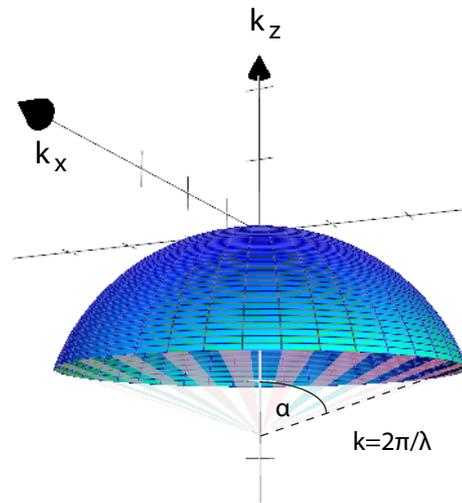
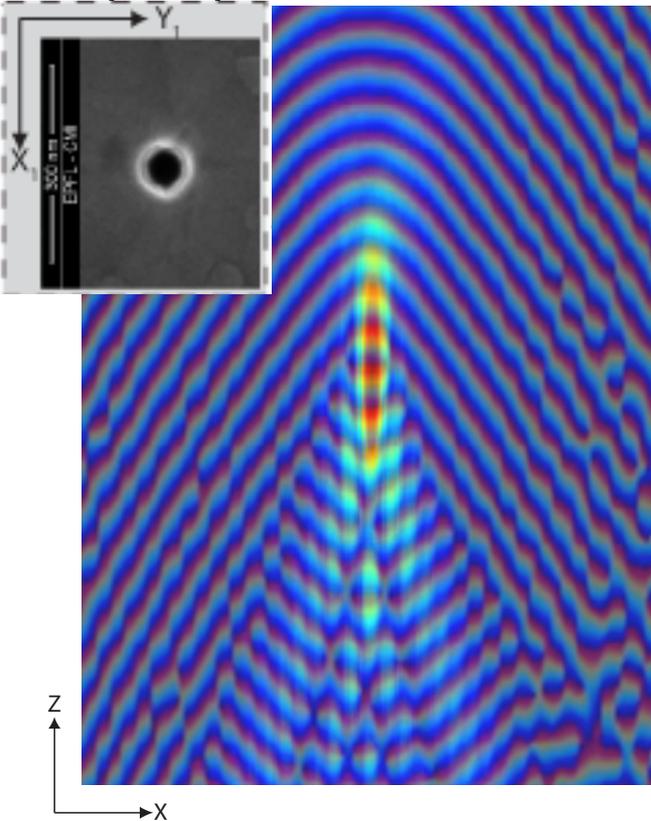


transmission



Experimental 3D Coherent transfer function

complex point source



Complex regularisation threshold

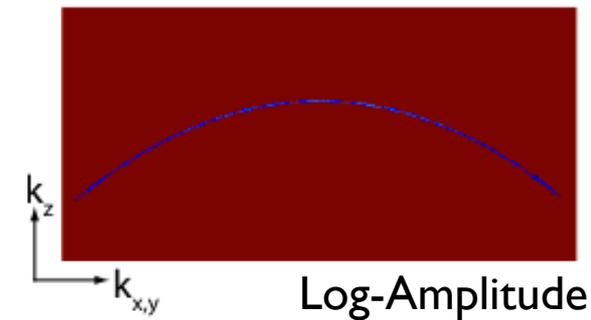
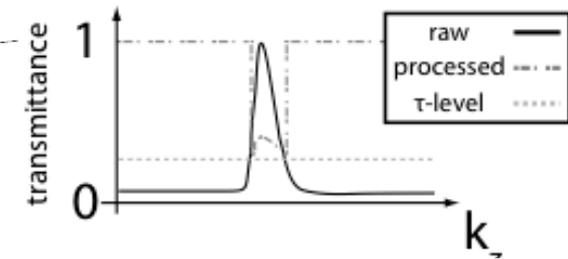


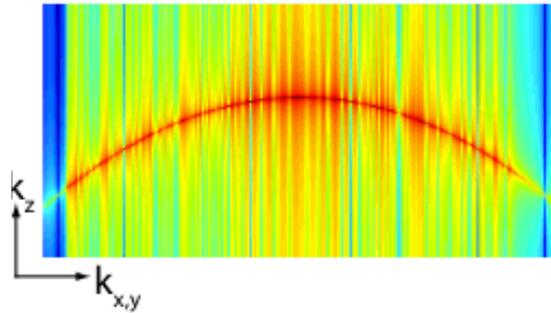
Fig. ▲ 3D Amplitude point spread function (APSF), phase (50%) and amplitude (50%)

Fig. ► 3D CTF [amplitude with a maximum subtended half-angle $\alpha = \arcsin(\text{NA}/n_{\text{immersion}})$].

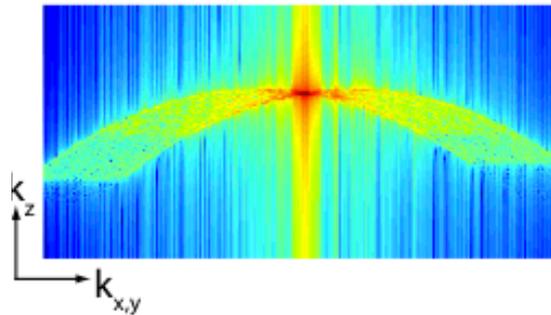
III. 3D COMPLEX DECONVOLUTION

3D complex deconvolution applied to scanning diffraction tomography.

Raw spectrum



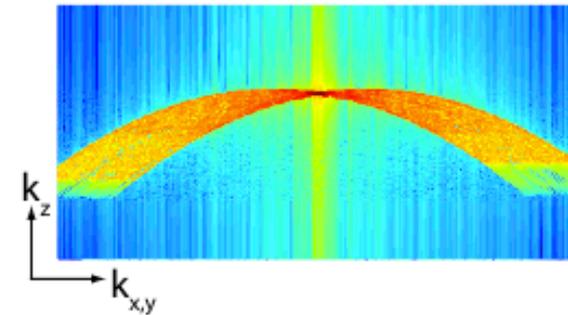
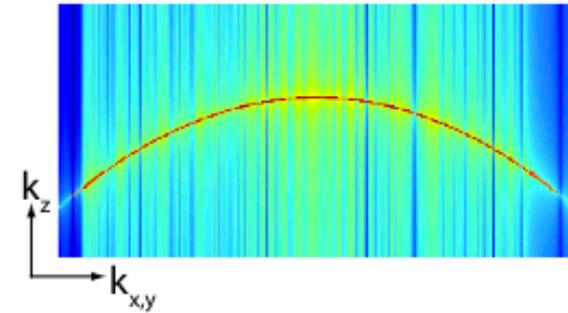
single acquisition



360° acquisition

Synthetic scattering potential

Complex deconvolved spectrum

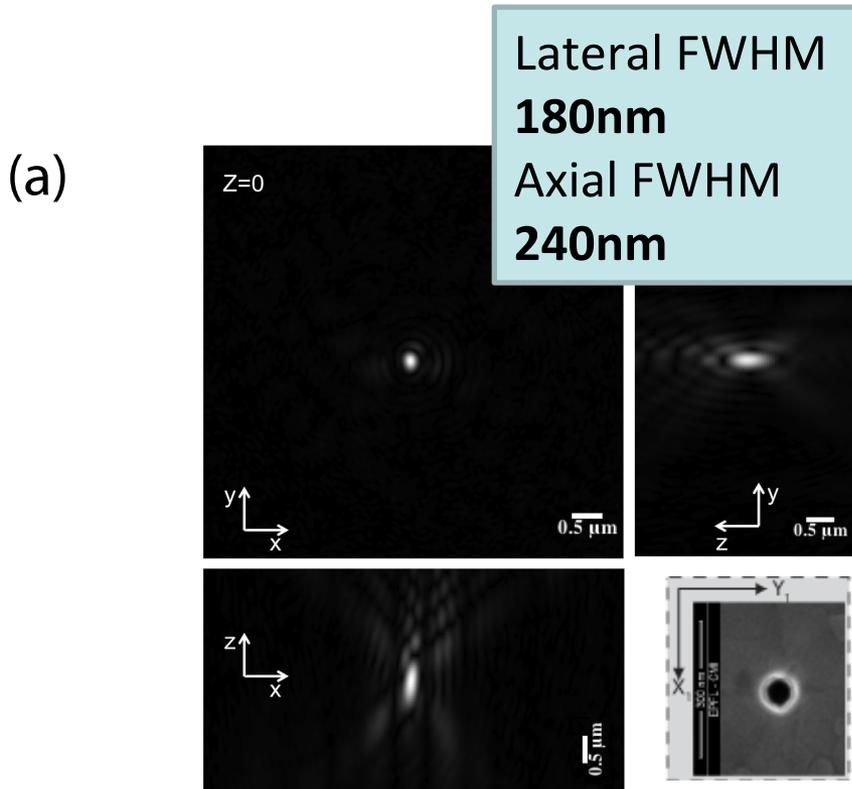


Complex deconvolved
Synthetic scattering potential

IV. Applications

APSF of 3D complex deconvolved diffraction tomography

Synthetic



Synthetic
+ Complex deconvolved

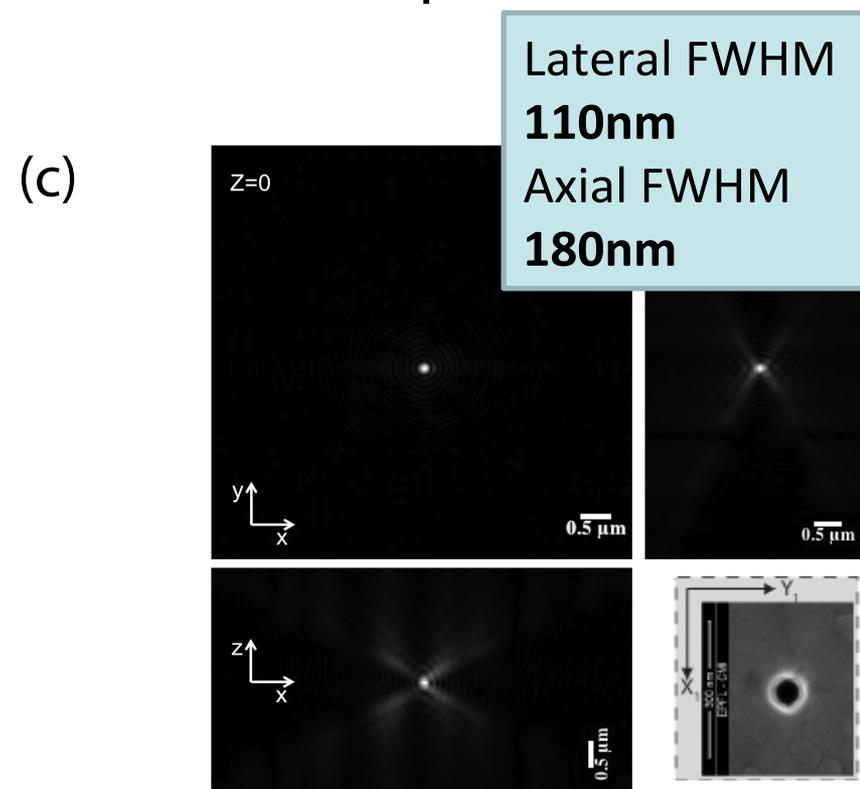


Fig. ▲ Characterization of angular scanning setup. Amplitude (a) and phase (b) show 3D APSF before, and (c)–(d) after 3D complex deconvolution

IV. Applications

APSF of 3D complex deconvolved diffraction tomography

Synthetic

Synthetic

+ Complex deconvolved

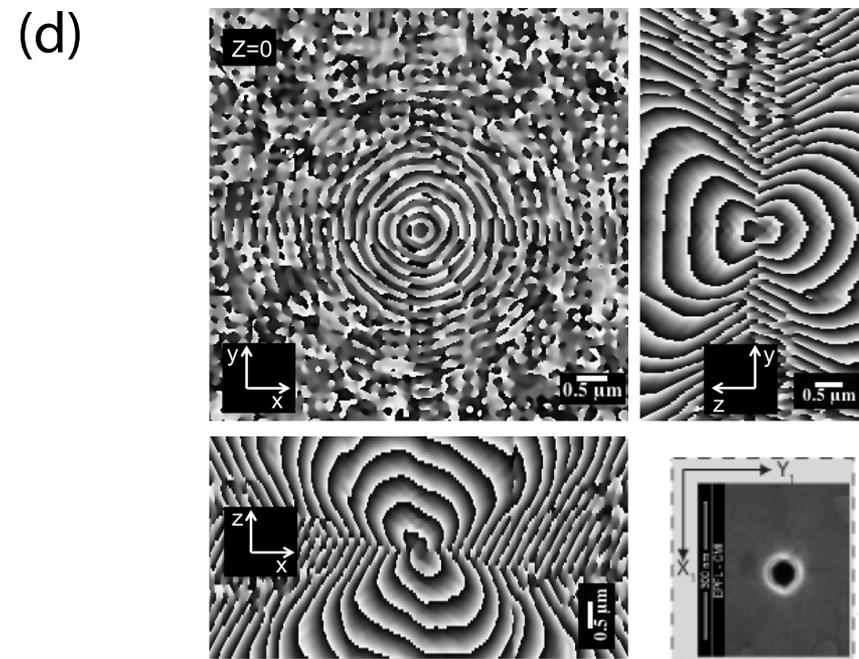
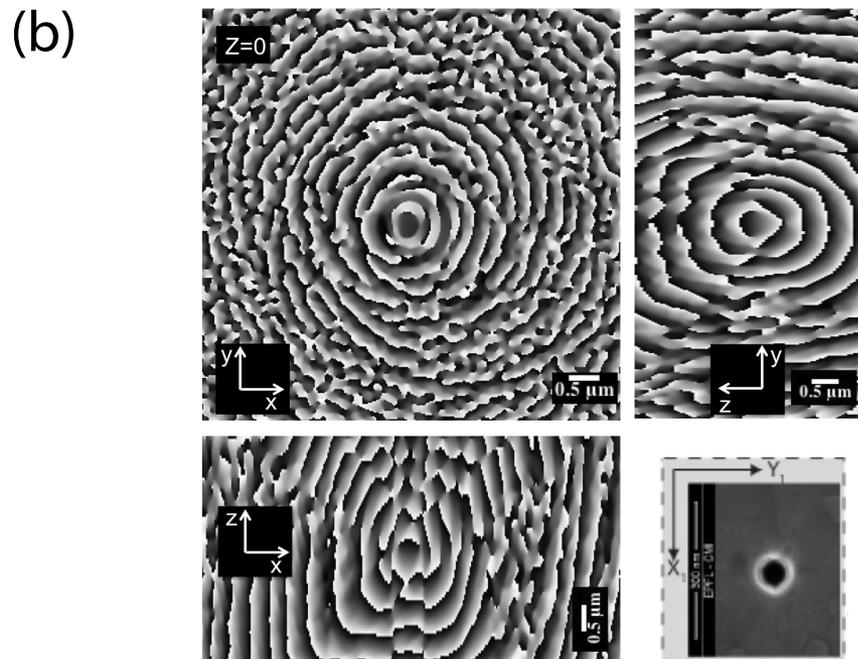


Fig. ▲ Characterization of angular scanning setup. Amplitude (a) and phase (b) show 3D APSF before, and (c)–(d) after 3D complex deconvolution

Experimental resolution assessment diffraction tomography

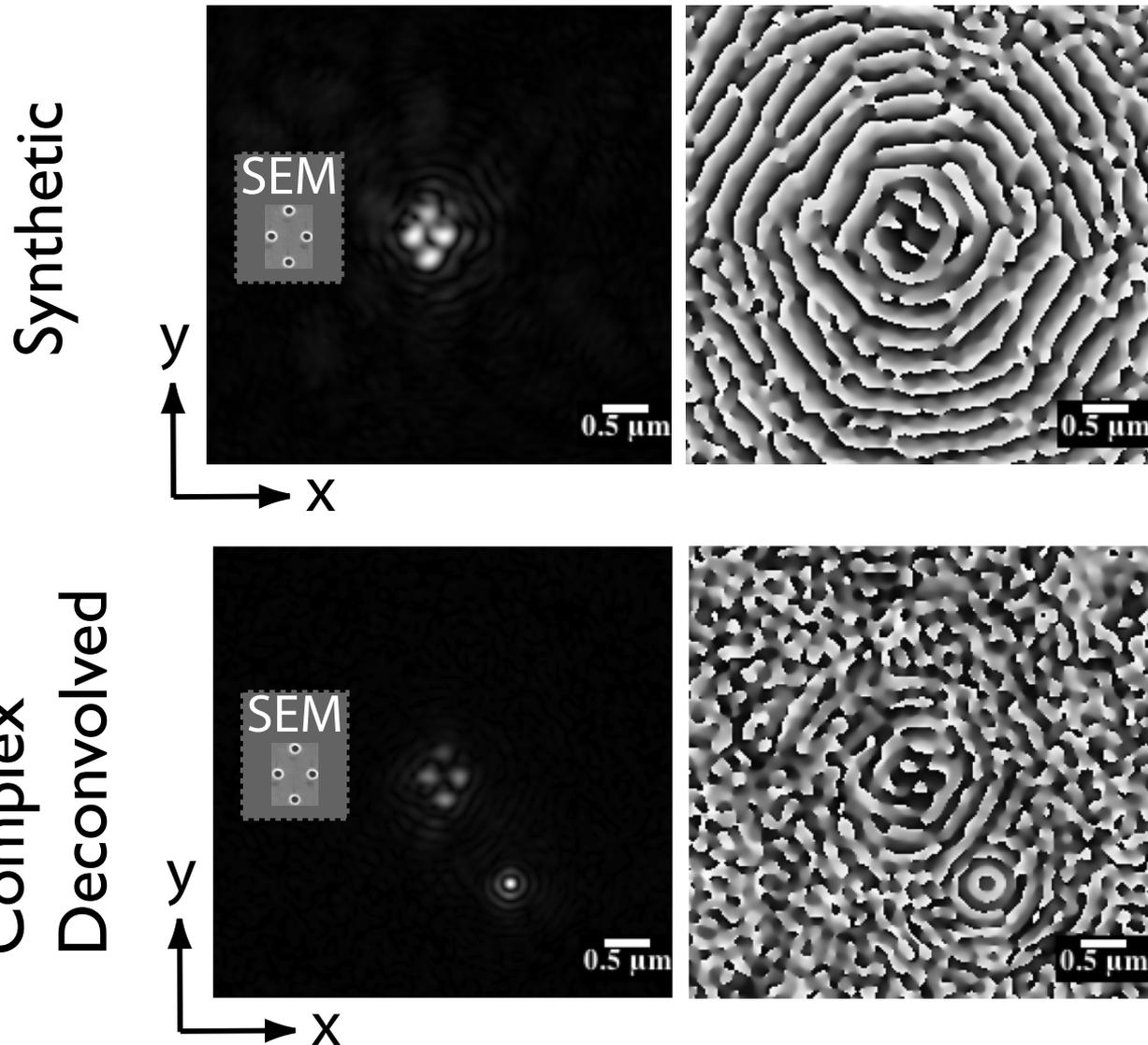
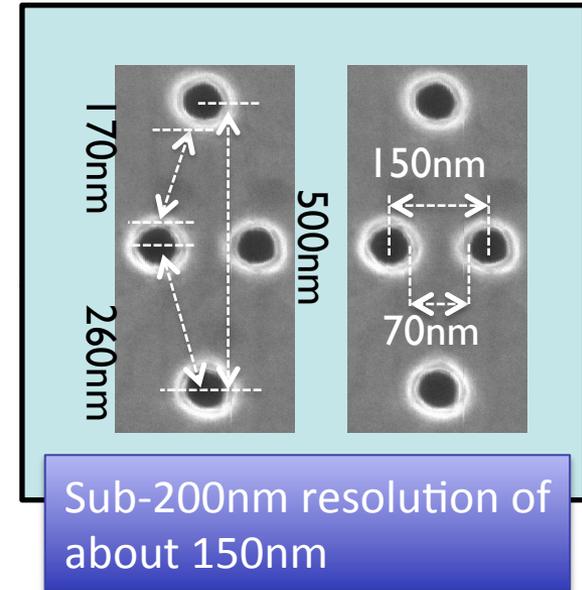
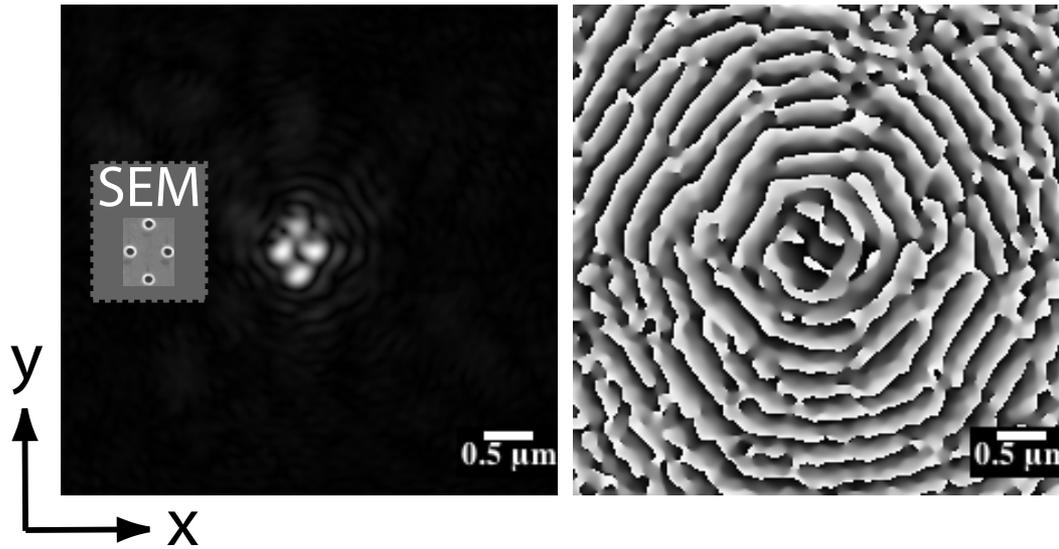


Fig. ◀ Four nano-holes (diameter=80nm) is depicted in amplitude (left) and phase (right) for $\eta_v = 500\text{nm}$, $\eta_h = 300\text{nm}$.

Experimental resolution assessment diffraction tomography

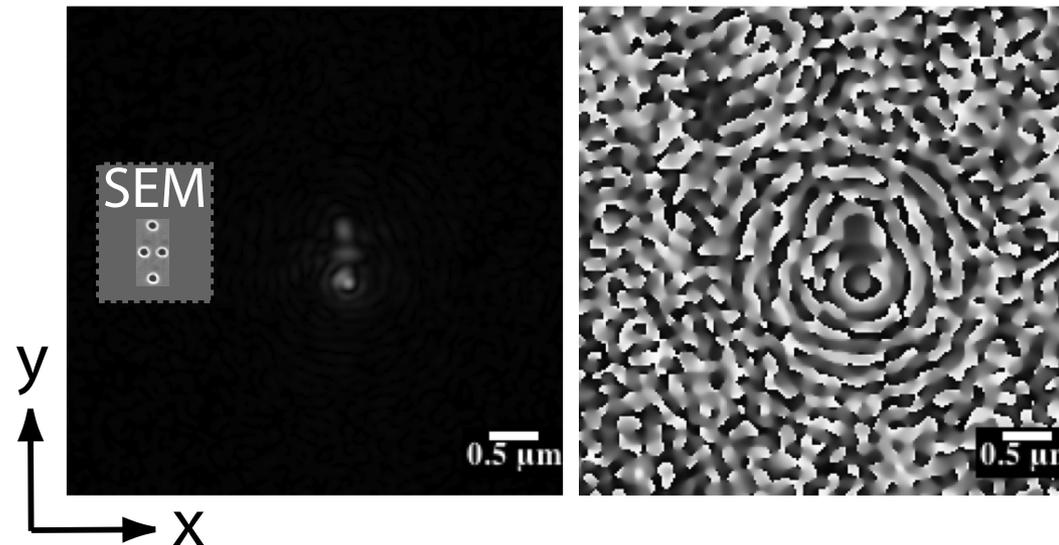
Synthetic



Sub-200nm resolution of about 150nm

Fig. ◀ Four nano-holes (diameter=80nm) is depicted in amplitude (left) and phase (right) for $\eta_v = 500\text{nm}$, $\eta_h = 150\text{nm}$ in (b).

Complex Deconvolved



IV. Applications

Resolution scale in neuronal axon phase imaging

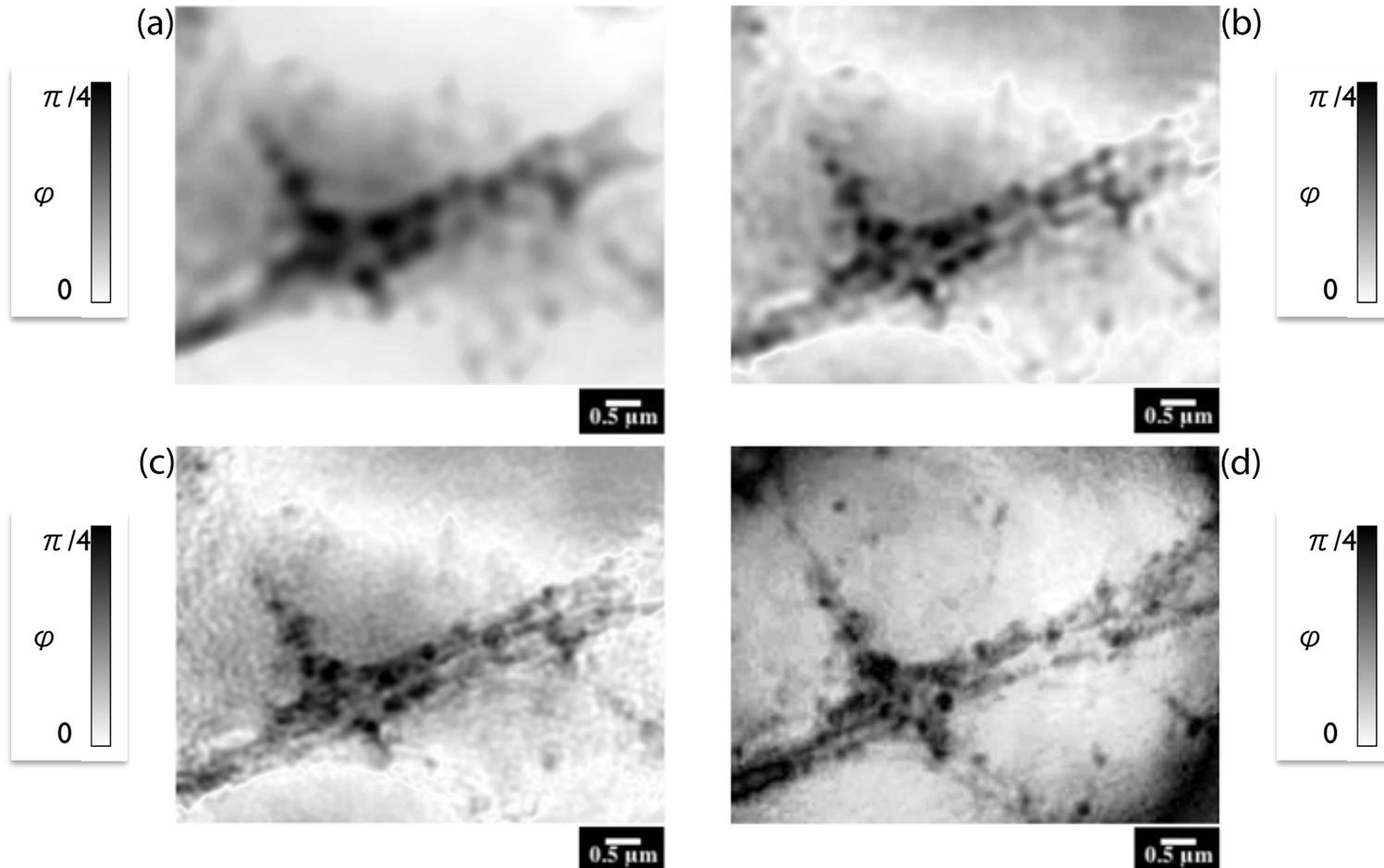


Fig. ▲ Fixed neurones. Phase images of an optical imaging system according to $\text{NA} = 0.7$ and $\lambda = 670\text{nm}$ in (a), of $\text{NA} = 0.95$ and $\lambda = 532\text{nm}$ in (b), and of $\text{NA} = 1.4$ (oil) and $\lambda = 405\text{nm}$ (c) and processed (d).

IV. Applications

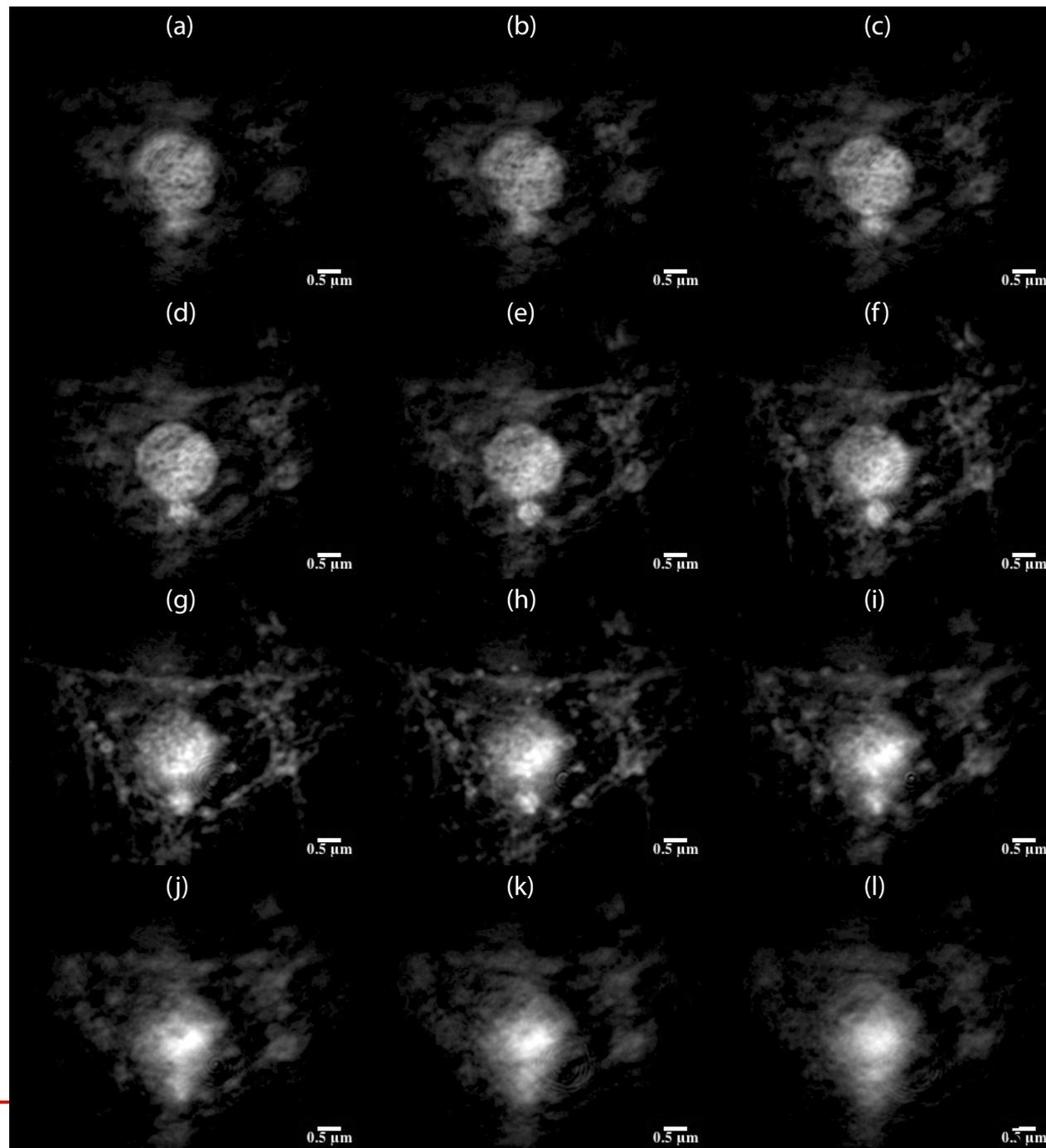
Optical sectioning of refraction index

Fig. ►

Complex deconvolved
refraction tomogram of
neuronal network. Images
(a)–(l) show lateral slices
through $3D - \text{Re}\{n\}$
(uncalibrated levels) with
respective distances

$\Delta z = 260\text{nm}$.

The sections go from top-to-
bottom and represent in
total a depth of $\approx 2.4\mu\text{m}$.



Deconvolved phase imaging for diffraction tomography

Theoretical Description

- Image formation and diffraction

Experimental methods

- DH tomography based on beam rotation
- 3D complex deconvolution

Main result:

A general scheme for **quantitative high resolution imaging** adaptable to all kind of acquisition methods

& QUESTIONS

V. ACKNOWLEDGEMENTS

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